## Electricity and Magnetism

Do <u>two</u> of the following three problems, each on a separate page (or pages) and write your name on every page you turn in.

## Problem 1

A thin insullating disk or radius a carries a uniform surface charge density  $\sigma$ . The disk is centered at the origin and lies in the x - y plane.



- **a.** Calculate the electric field on the *z*-axis.
- **b.** Calculate the electric potential on the *z*-axis.
- c. Verify that  $\overrightarrow{E} = -\nabla V$ .

## Problem 2

A small circular wire loop of radius a is located at the center of a much larger circular wire loop of radius b, as shown below. Find the mutual inductance of the loops assuming that  $a \ll b$ .



## Problem 3

Two point charges, each of magnitude q, are situated a distance h and h/2, respectively, located above each other on an axis normal to an infinite conducting xy plane. What is the charge density  $\sigma$  on top of the plane as a function of the cylindrical radius s?